

FIG. 1

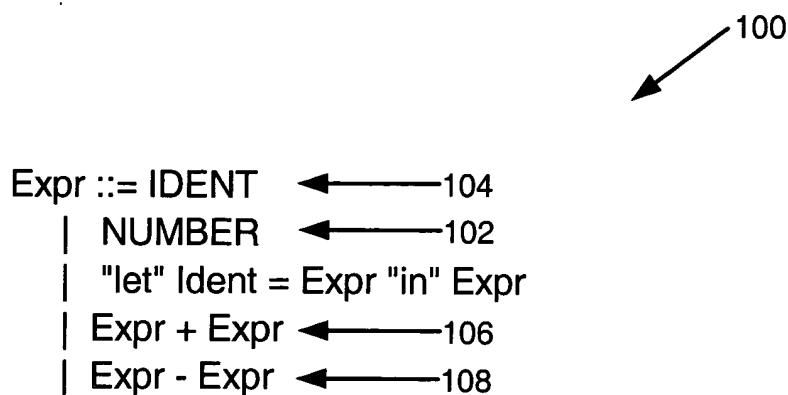


FIG. 2

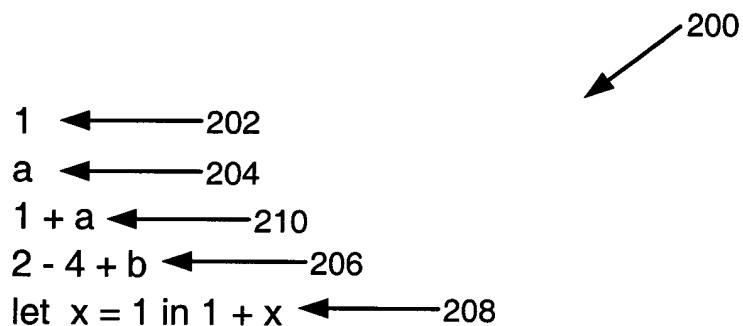


FIG. 3

```
abstract structure Exp ← 314
  case Const ← 306
    val as Integer
  case Bin ← 308
    op as Op
    left as Exp ← 302
    right as Exp ← 304
  case Let ← 310
    name as Name
    def as Exp
    body as Exp
  case Var
    name as Name

enum Op
  Add
  Sub

type Name = String
```

300

FIG. 4

```
structure Exp
  public override ToString() as String?
    match me
      x as Const:
        return ToString(x.val)
      x as Bin:
        return "(" + x.left + ToString(x.op) + x.right + ")"
      x as Let:
        return "(let " + x.name + "=" + x.def + " in " + x.body +
      ")"
      x as Var:
        return x.name

  ToString(o as Op) as String?
    match o
      Add: return "+"
      Sub: return "-"
```

400

FIG. 5

```

Closed(e as Exp) as Boolean
return Closed(e, {}) ← 510

type BoundedNames = Set of Name ← 512
Closed(e as Exp, ns as BoundedNames) as Boolean
match e ← 502
  Const(_): return true ← 504
  Bin(_,l,r): return Closed(l, ns) and Closed(r, ns) ← 518
  Let(n,d,b): return Closed(d, ns) and Closed(b, ns + {n}) ← 514
  Var(n): return n in ns ← 506
  516
  508

```

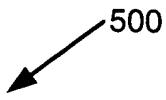
500


FIG. 6

```

Eval(e as Exp) as Integer
require Closed(e, {})
return Eval(e, {->})

type Environment = Map of Name to Integer
Eval(e as Exp, env as Environment) as Integer
require Closed(e, Indices(env))
match e
  Const(v): return v
  Bin(o,l,r): return Eval(o, Eval(l, env), Eval(r, env))
  Let(n,d,b): return Eval(b, env + {n -> Eval(d, env)}) ← 600
  Var(n): return env(n)

Eval(o as Op, l as Integer, r as Integer) as Integer
match o
  Add: return l + r
  Sub: return l - r

```

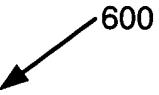
600


FIG. 7

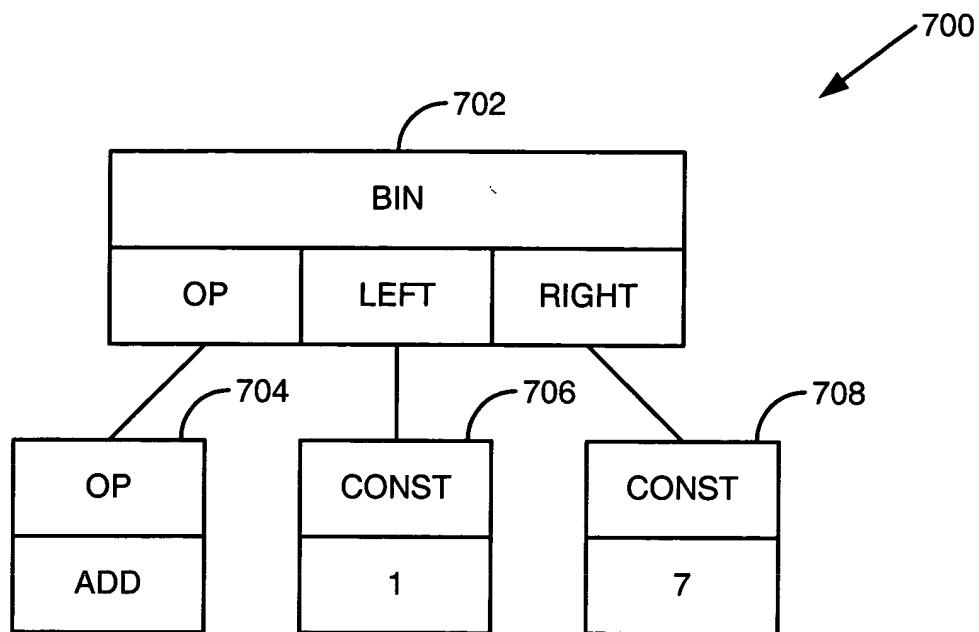


FIG. 8

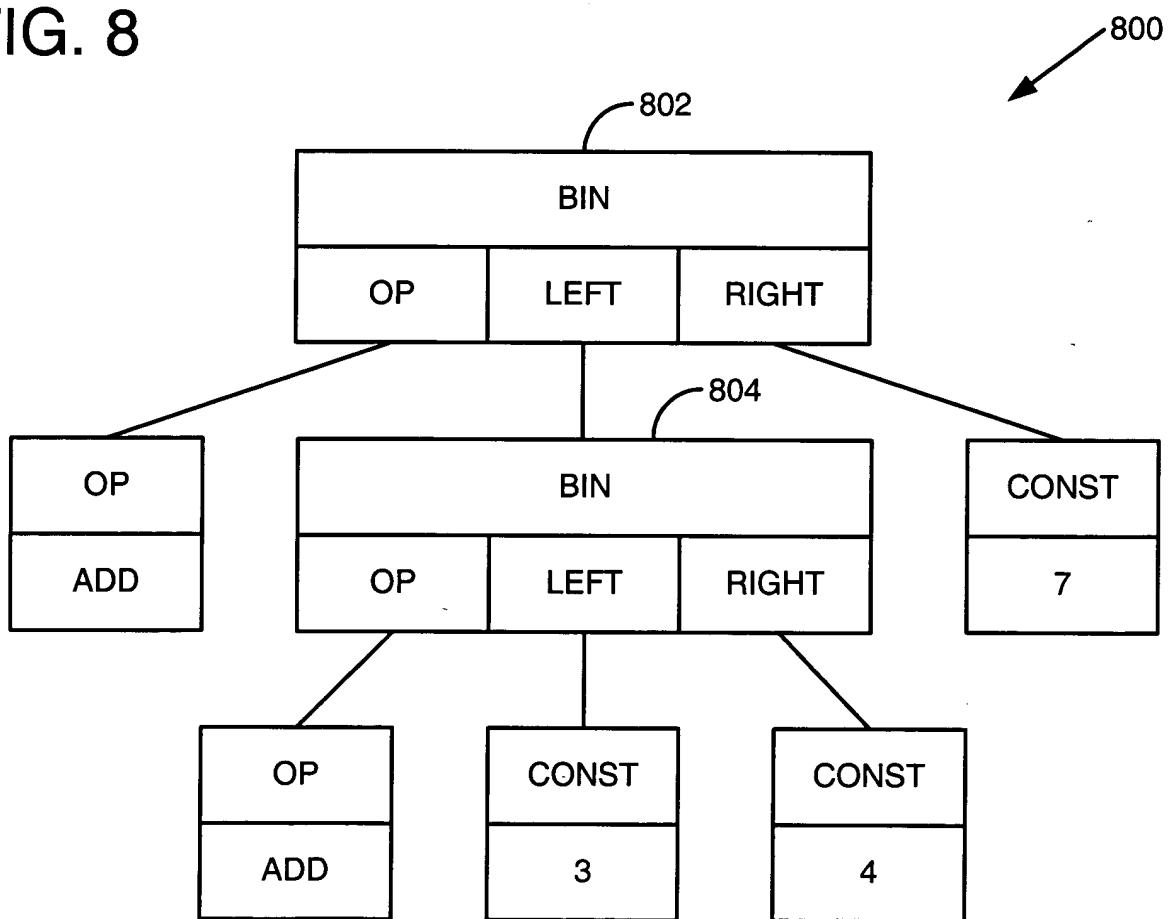


FIG. 9

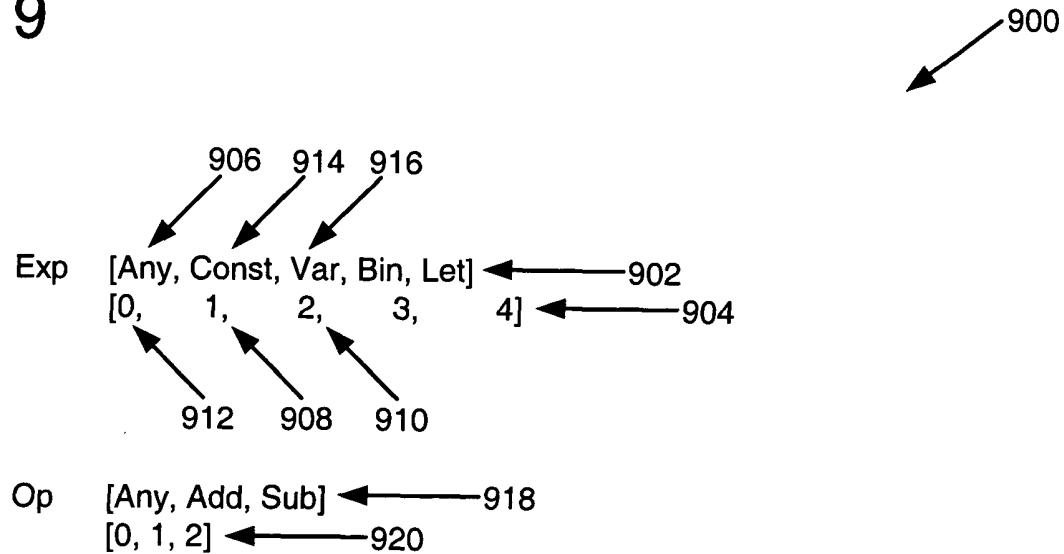


FIG. 12

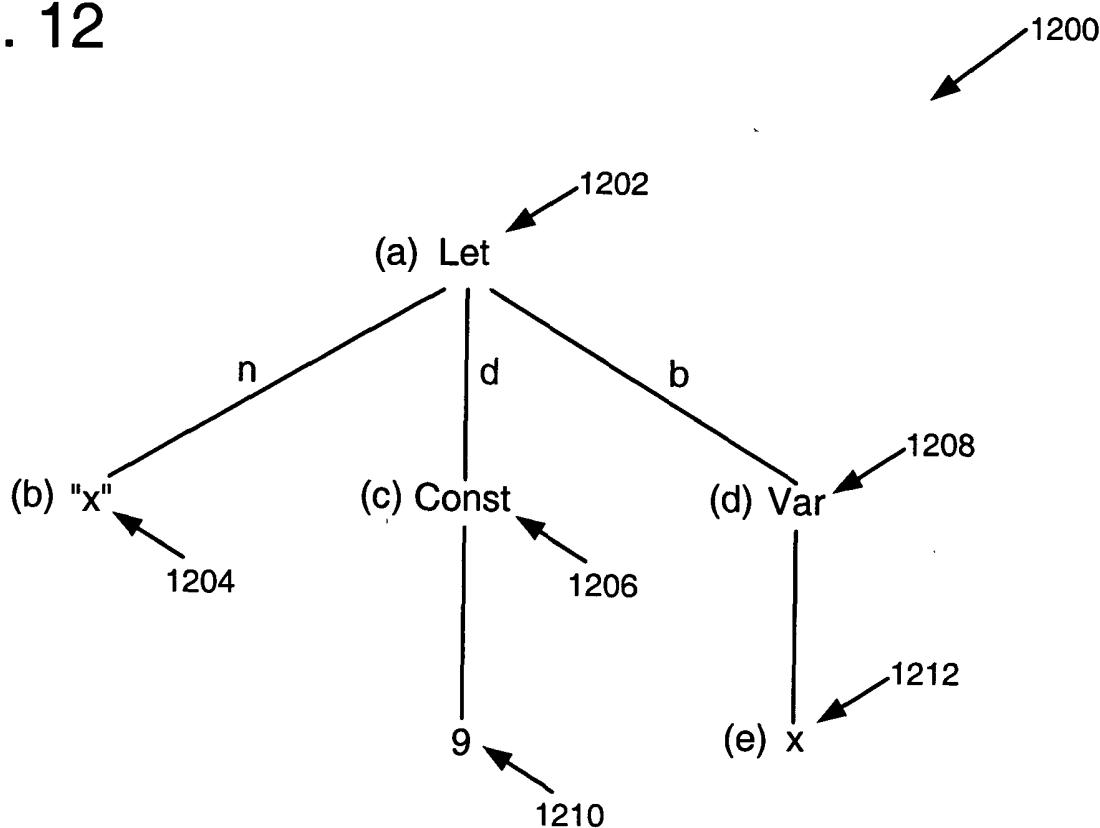


FIG. 10

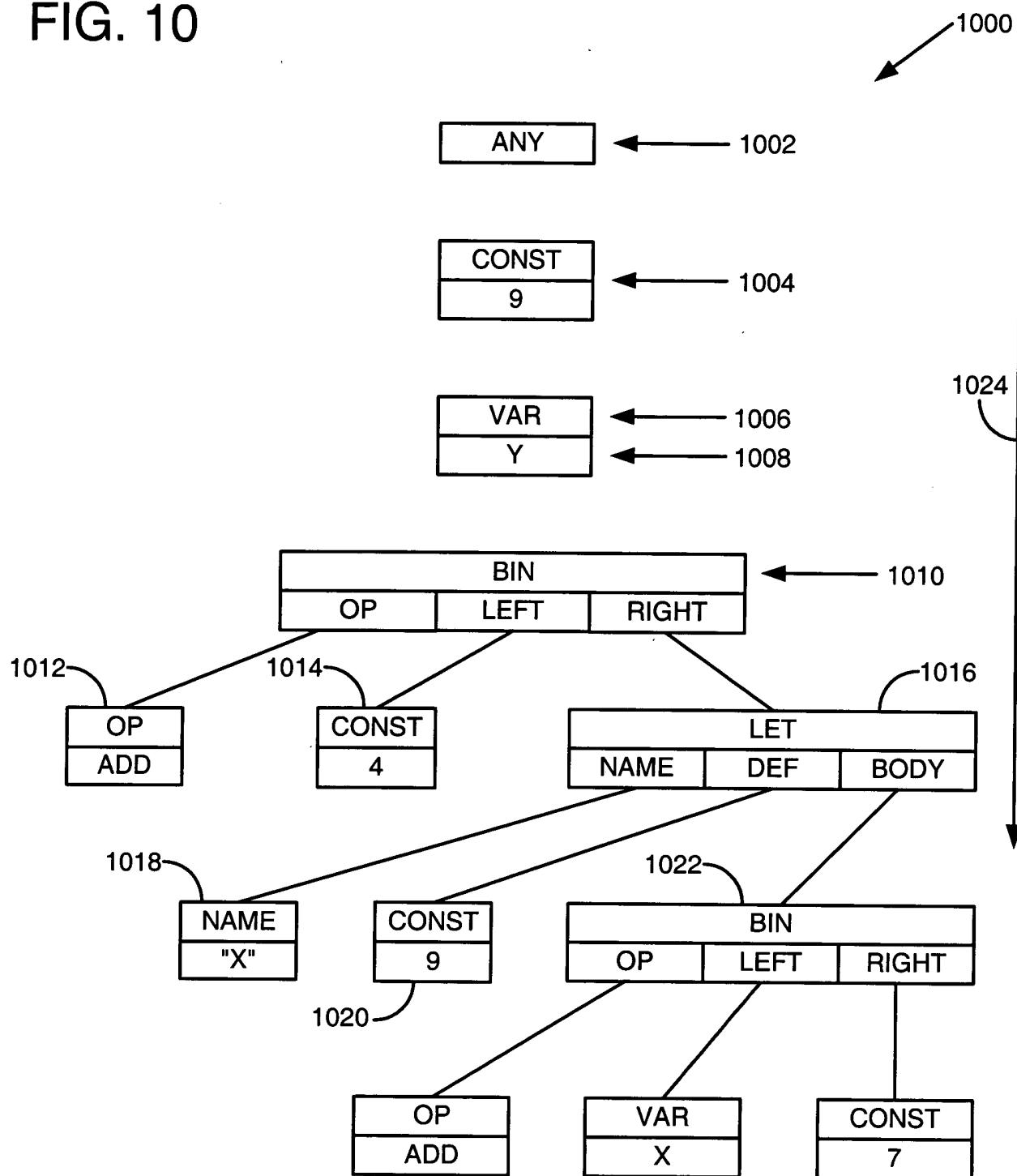
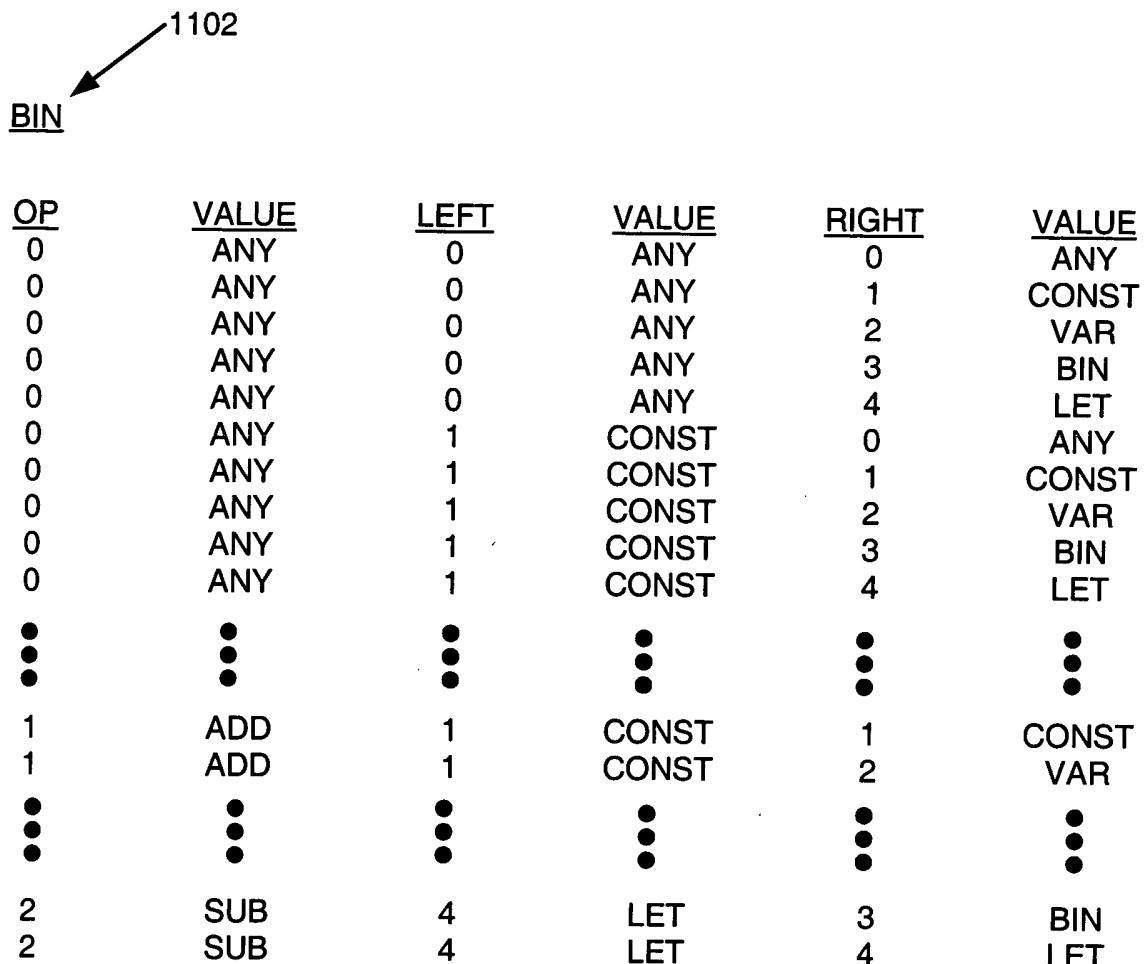


FIG. 11



<u>OP</u>	<u>VALUE</u>	<u>LEFT</u>	<u>VALUE</u>	<u>RIGHT</u>	<u>VALUE</u>
0	ANY	0	ANY	0	ANY
0	ANY	0	ANY	1	CONST
0	ANY	0	ANY	2	VAR
0	ANY	0	ANY	3	BIN
0	ANY	0	ANY	4	LET
0	ANY	1	CONST	0	ANY
0	ANY	1	CONST	1	CONST
0	ANY	1	CONST	2	VAR
0	ANY	1	CONST	3	BIN
0	ANY	1	CONST	4	LET
•	•	•	•	•	•
•	•	•	•	•	•
1	ADD	1	CONST	1	CONST
1	ADD	1	CONST	2	VAR
•	•	•	•	•	•
•	•	•	•	•	•
2	SUB	4	LET	3	BIN
2	SUB	4	LET	4	LET

FIG. 13

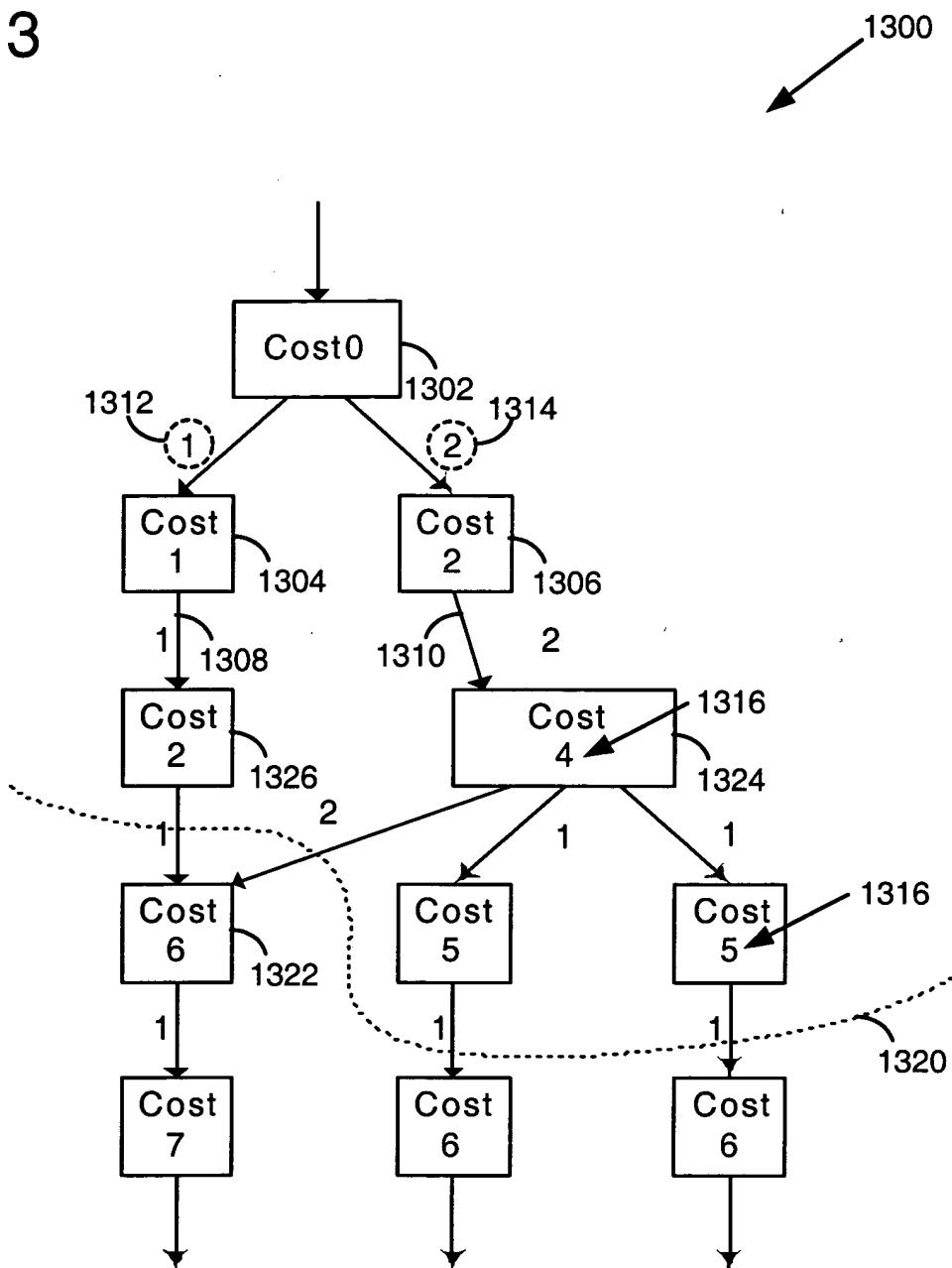


FIG. 14

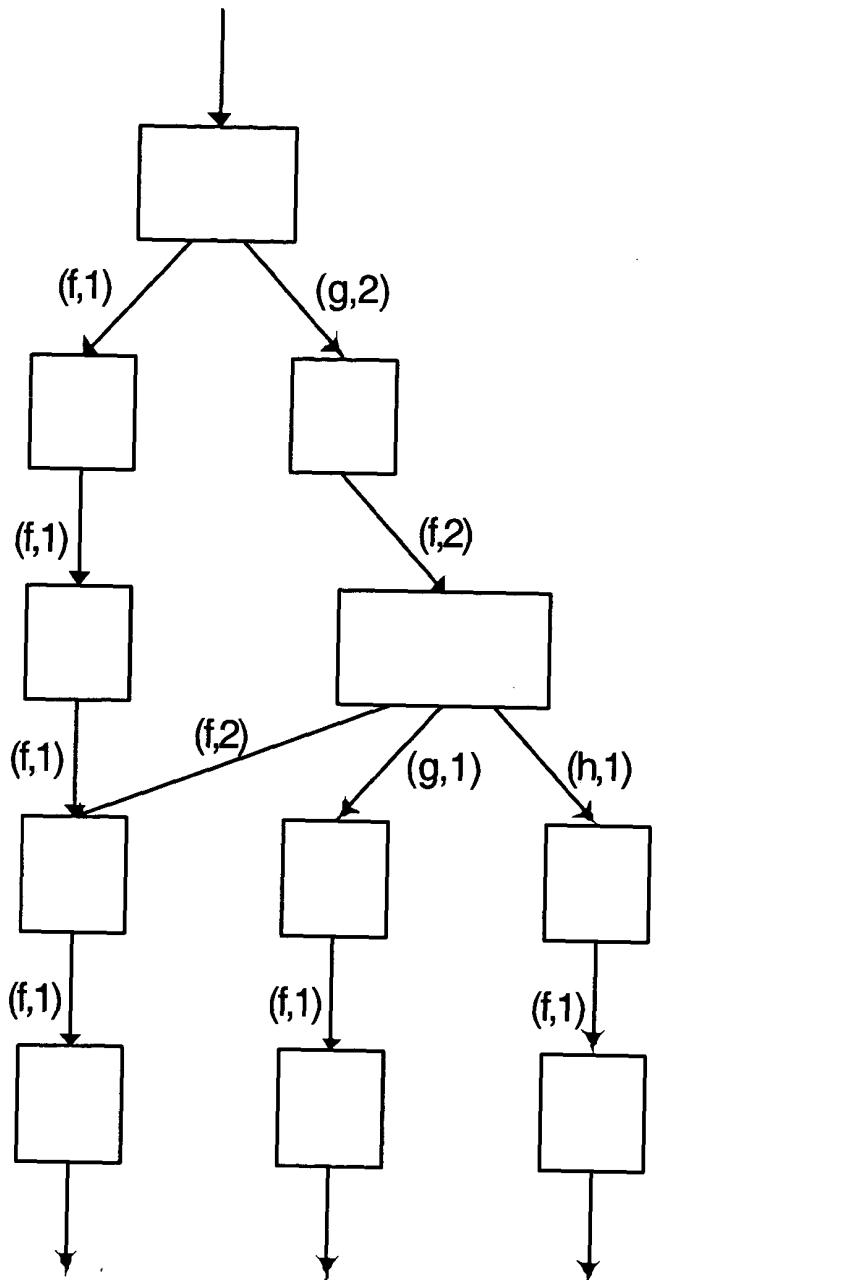


FIG. 15

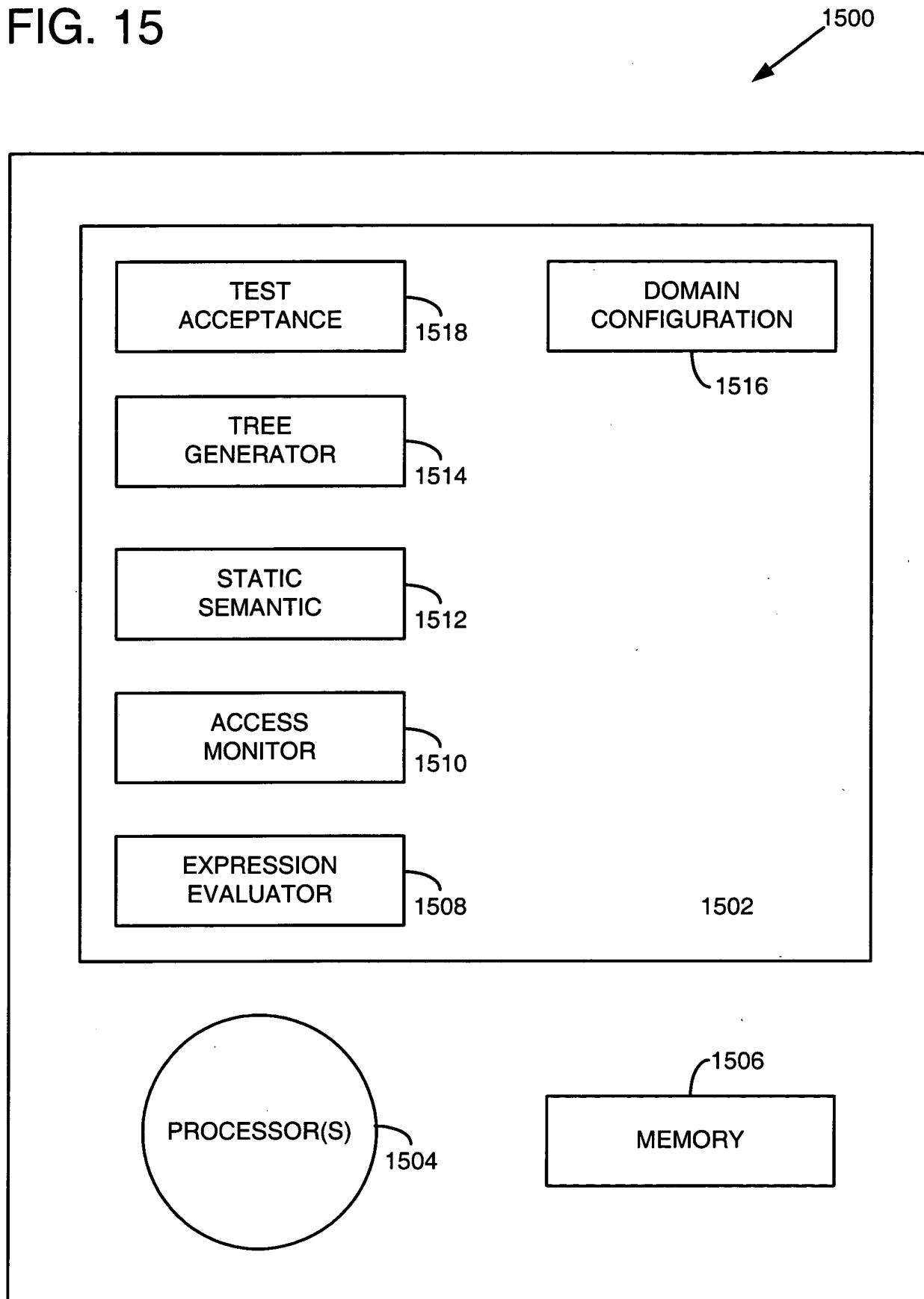


FIG. 16

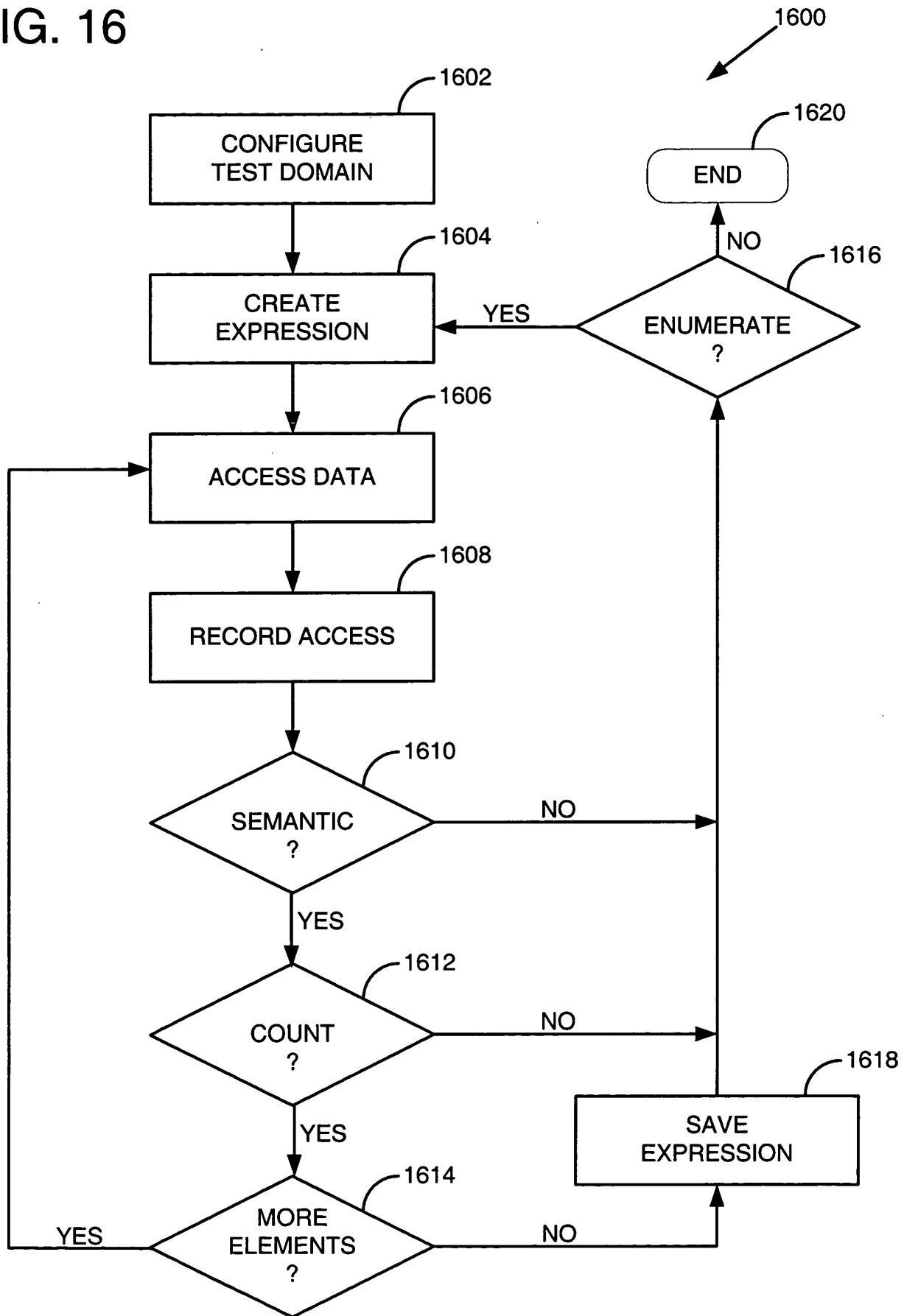


FIG. 17

```
abstract structure Exp
  case Const ~ 1710
  val as Integer ~ 1711
  case Bin ~ 1720
  op as Op ~ 1721
  left as Exp ~ 1722
  right as Exp ~ 1723
  case Let ~ 1730
  name as Name ~ 1731
  def as Exp ~ 1732
  body as Exp ~ 1733
  case Var ~ 1740
  name as Name ~ 1741

enum Op
  Add
  Sub

type Name = String
```

1700 →

1750 →

1760 →

FIG. 18

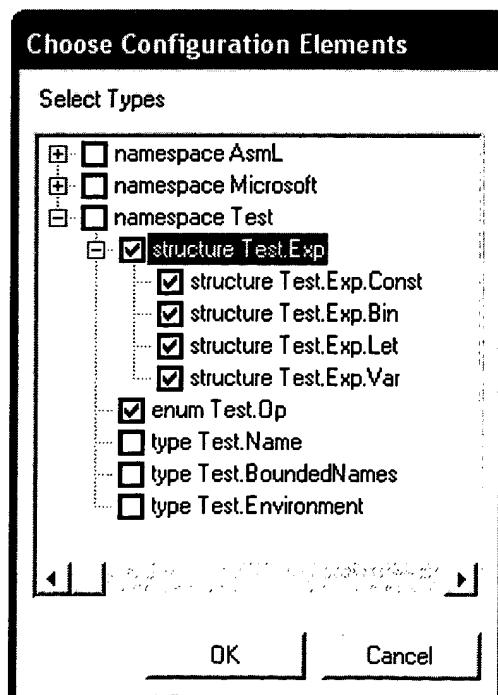


FIG. 19

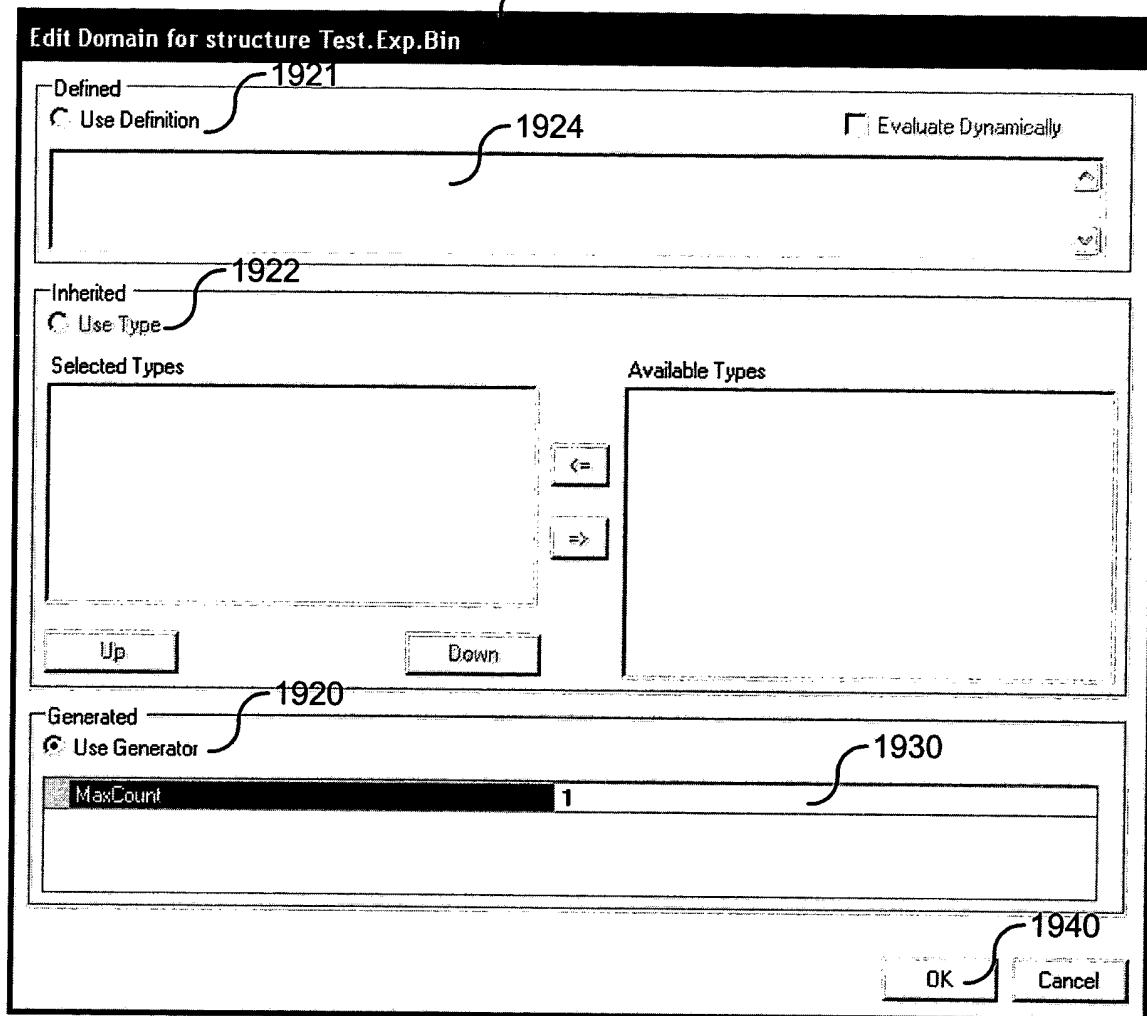


FIG. 20

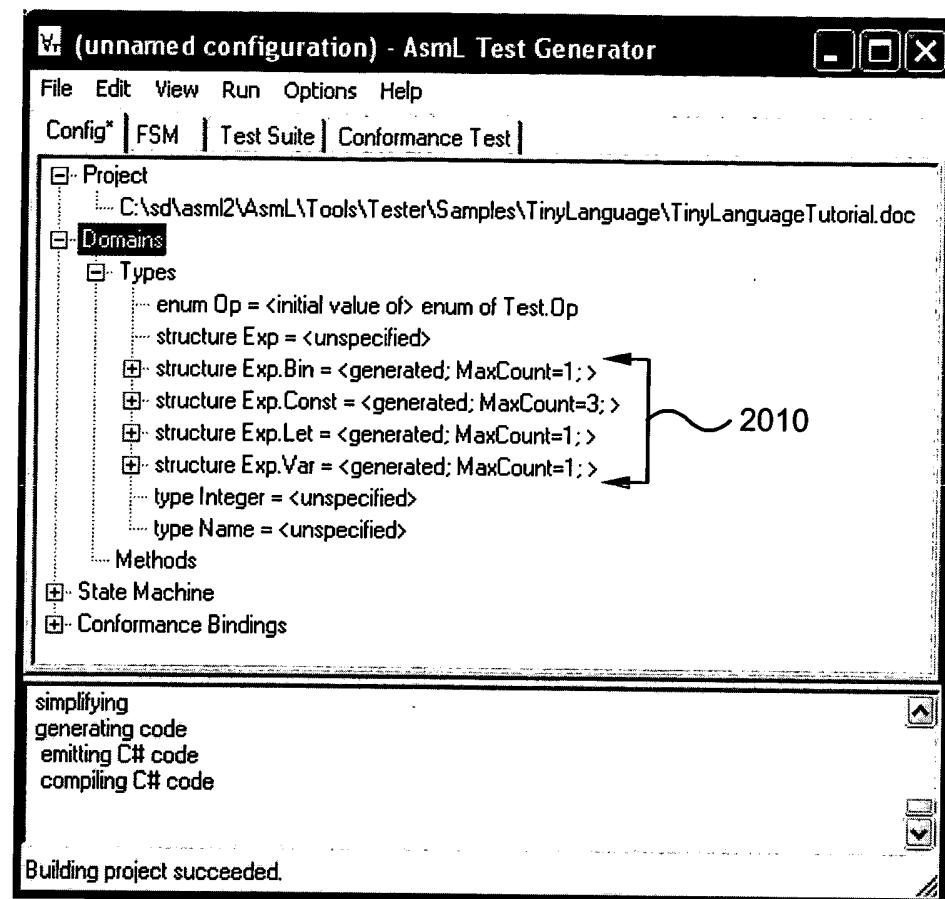


FIG. 21

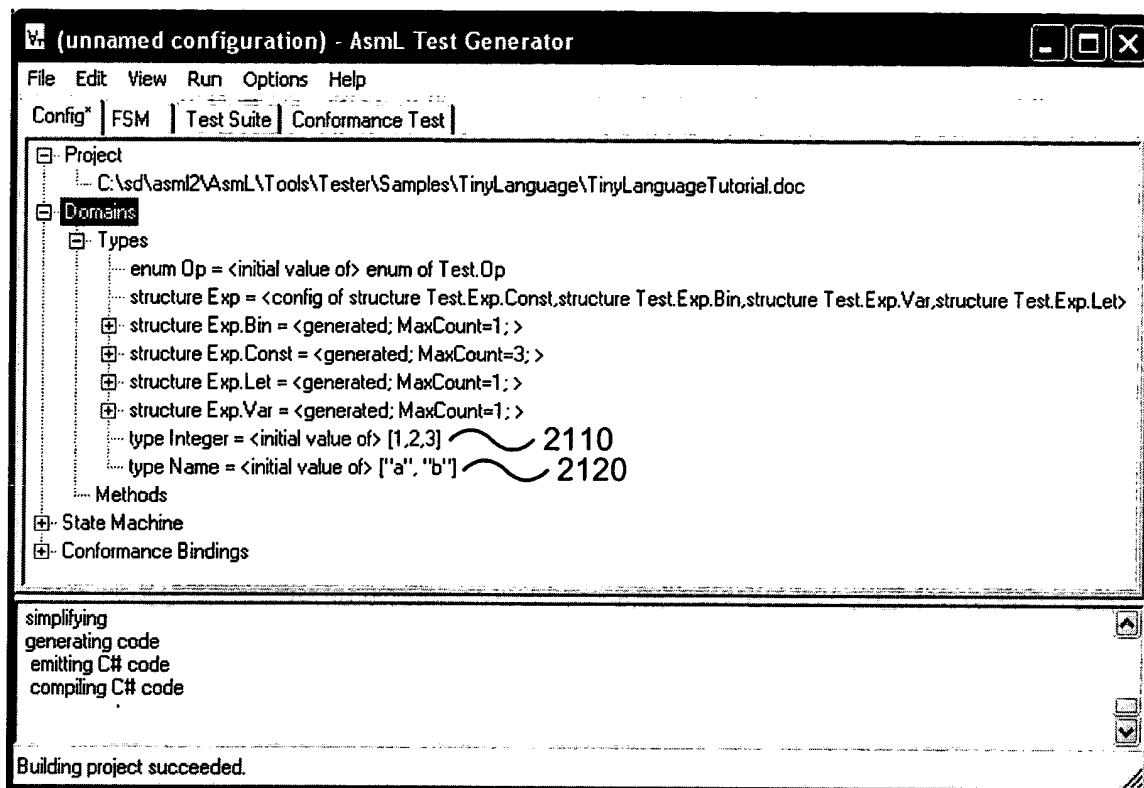


FIG. 22

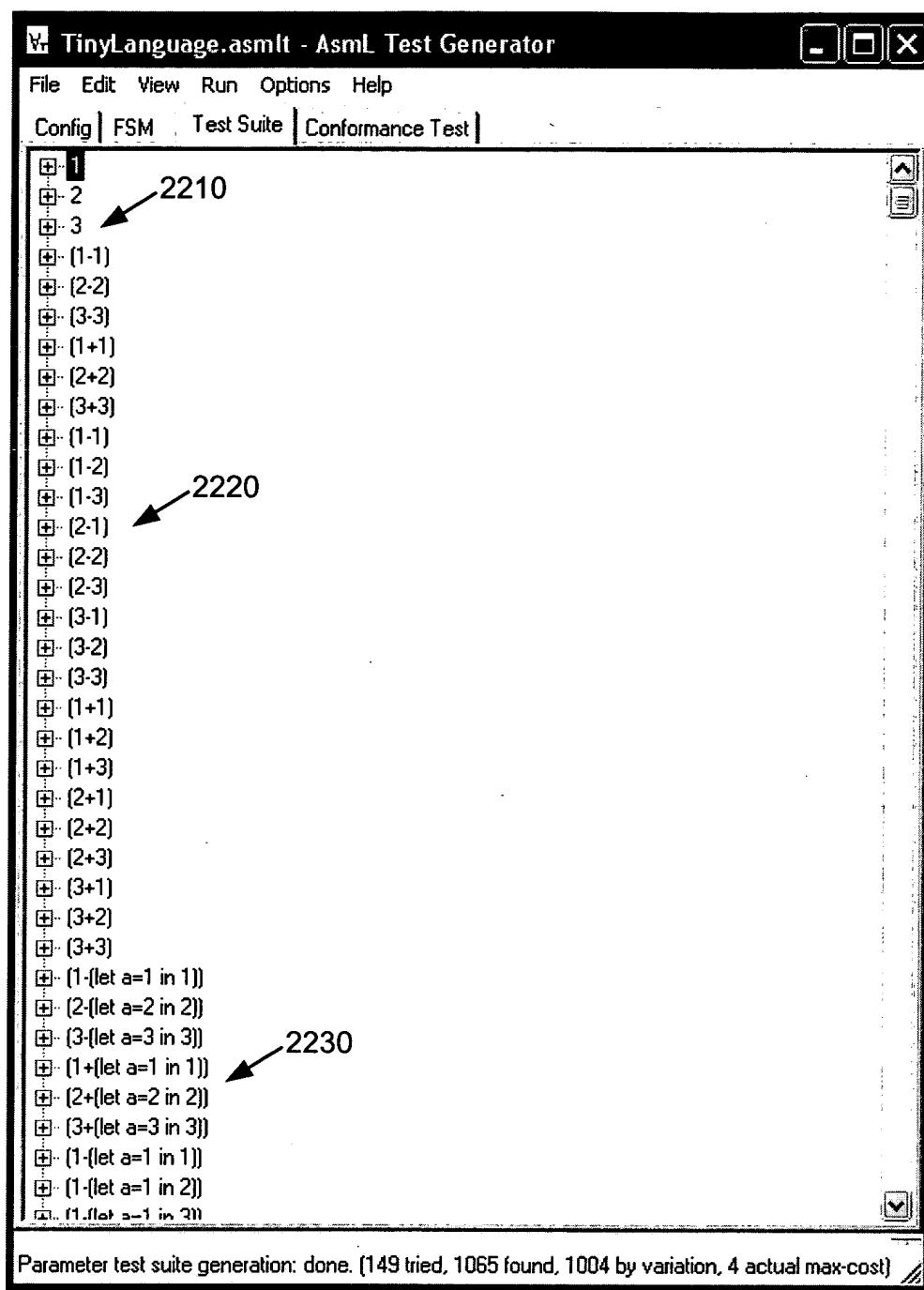


FIG. 23

